

Exercises Condensed Matter Physics (Experimentalphysik 5c), WS16/17

1) Derivative of the Fermi-Dirac distribution (2 credits)

Show for a free electron gas, that

$$\frac{\partial f_0}{\partial k_x} = \frac{\partial f_0}{\partial E} \hbar v_x$$

2) Conductivity of a metal within Boltzmann transport theory (2 credits)

Show the missing steps in the derivation of the conductivity as discussed in the lecture

$$\sigma = \frac{e^2 \tau(E_F)}{m^*} n$$

3) Thermocouple (1 credits)

In experimental or technical set-ups the temperature is often measured using a thermocouple, i.e. two wires of different metals (with different Seebeck coefficients S), which are electrically connected at the position, where the temperature T should be measured. The resulting voltage V_{th} at the open ends of the wires is measured at room temperature (300K), from which T can be determined.

Using an Fe/ Ni thermocouple a thermoelectric voltage of $V_{th} = 25\text{mV}$ is obtained. Calculate the corresponding temperature T .

(Seebeck coefficients are typically given relative to Cu or Pt. $S_{Ni-Cu} = -22 \mu\text{V/K}$, $S_{Fe-Cu} = 10 \mu\text{V/K}$.)

4) 4-probe resistivity measurement (3 credits)

To avoid contributions of wire and contact resistivity in precession resistivity measurements the so called 4-probe technique is used: On each end of the sample wires are attached through which a current of 10mA is sent through the sample. With a second pair of wires a voltage V is measured using a high ohmic voltmeter ($1\text{M}\Omega$). Which voltage U is obtained and which specific resistivity of the sample results from this measurement?

(probe wires: resistivity $\rho_{Cu} = 1.7\mu\Omega\text{cm}$, diameter 0.5mm^2 , lengths $l = 3\text{m}$; specific sample resistivity $\rho_{\text{sample}} = 100\mu\Omega\text{cm}$, sample dimensions $3.0 \times 0.5 \times 0.1 \text{ mm}^3$)

